



TECHNO INDIA GROUP PUBLIC SCHOOL

JEE MOCK TEST (Series II)

Paper Part – 4

Time: 3 hours

PHYSICS

F.M.: 300

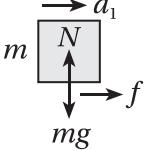
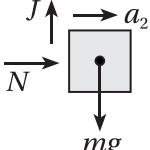
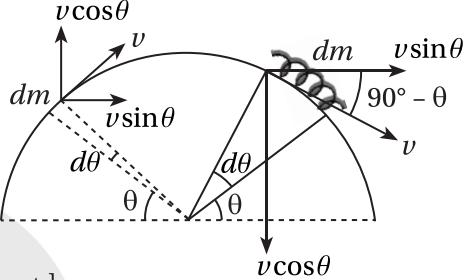
ANSWERS

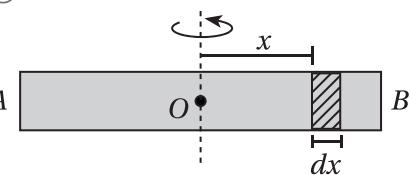
SECTION A

Section A consists of 20 questions of 4 mark each.

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| 1. | <p>①</p> $y = (10 \sin 30^\circ)t - \frac{1}{2} \cdot \frac{g}{\sqrt{2}} \cdot t^2 = 0 \Rightarrow t = \sqrt{2} \text{ s}$ <p>$\left[y = (u \sin \alpha)t - \frac{1}{2} \cdot (g \cos \theta) \cdot t^2 \text{ and put } y = 0 \right]$</p> | |
| 2. | <p>②</p> $a = \frac{1}{2} \frac{d(v^2)}{ds} = \frac{1}{2} \times \left(-\frac{2}{5} \right) = -0.2 \text{ m/s}^2$ | |
| 3. | <p>③</p> $[k_B \theta] = \text{energy} = ML^2 T^{-2} = [\alpha]L \quad \therefore [\alpha] = MLT^{-2}$ $[P] = \frac{[\alpha]}{[\beta]} = M \cdot \frac{L}{T^2} \cdot \frac{1}{L^2} = ML^{-1} T^{-2} \quad \therefore [\beta] = \frac{MLT^{-2}}{ML^{-1} T^{-2}} = M^0 L^2 T^0$ | |
| 4. | <p>②</p> $\nu_1 \cos \theta_1 = \nu_2 \cos \theta_2 \quad \therefore \frac{\nu_1}{\nu_2} = \frac{\cos 60^\circ}{\cos 30^\circ} = \frac{1}{\sqrt{3}}$ | |
| 5. | <p>③ (after cut)</p> $m_1 a_1 = kx$ $kx = T$ $\therefore m_1 a_1 = kx = T = m_2 g$ $a_1 = \left(\frac{m_2}{m_1} \right) g$ <p>m_2 is shown with a vertical arrow pointing upwards labeled T, and a vertical arrow pointing downwards labeled $m_2 g$. The acceleration $a_2 = 0$ is noted as initially before cut.</p> | |

[2]

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| 6. | <p>③ Case (1): $f = ma_1 \quad f \leq \mu N$ $ma_1 \leq \mu mg \Rightarrow a_1 \leq \mu g$</p>  <p>Case (2): $N = ma_2 \quad f \leq \mu N$ $f = mg \Rightarrow mg \leq \mu N \Rightarrow mg \leq \mu ma_2 \Rightarrow a_2 \geq (g/\mu)$</p>  | | |
| 7. | <p>② $(0.5 + 0.25)(20) \times (10 \text{ N}) \cos 60^\circ = W_1 = 15 \times 5 = 75$ $(0.25)(20) \times 10 \cos 60^\circ = W_2 = 25 \text{ J} \quad 75 : 25 = 3 : 1$</p> | | |
| 8. | <p>④ $\vec{p} = \frac{mv}{\pi} \int_0^\pi \sin \theta d\theta \cdot \hat{i} = \frac{2mv}{\pi} \hat{i}$</p> <p>Note: $dm = \frac{m}{\pi R} \cdot R d\theta = \frac{m}{\pi} d\theta$</p> $d\vec{p} = \int (dm)(v \sin \theta \hat{i}) \quad [v \cos \theta \text{ part will be canceled out.}]$ |  | |
| 9. | <p>① $v_1 = \sqrt{2 \times 10 \times 5} \Rightarrow 10(-j) \text{ m/s}$ $v_2 = \sqrt{2 \times 10 \times \frac{4}{5}} = 4 \text{ m/s } (\hat{j})$ $\Delta \vec{p} = m(\vec{v}_2 - \vec{v}_1) = 14 \hat{j} \text{ kg m/s}$</p> | | |
| 10. | <p>② $mv_0 \cos \theta = (M+m)v \Rightarrow v = \frac{mv_0 \cos \theta}{M+m}$</p> | | |
| 11. | <p>① Step 1: $\frac{GMm}{r^2} = m\omega^2 r \quad \text{and} \quad \omega = \frac{2\pi}{T} \quad \therefore T = 2\pi \sqrt{\frac{r^3}{GM}}$... (1)</p> <p>Step 2: by applying conservation of energy</p> $\frac{1}{2} m \left(\frac{dx}{dt} \right)^2 - \frac{GMm}{x} = -\frac{GMm}{r} \Rightarrow \left(\frac{dx}{dt} \right) = \left[\frac{2GM}{r} \left(\frac{r-x}{x} \right) \right]^{1/2}$ $\Rightarrow \left(\frac{2GM}{r} \right)^{1/2} \int_0^t dt = \int_0^r \left(\frac{x}{r-x} \right)^{1/2} dx \quad \text{for integration use } x = r \sin^2 \theta$ $\Rightarrow \left(\sqrt{\frac{2GM}{r}} \right) t = \frac{\pi r}{2} \quad t = \frac{\pi r}{2} \cdot \left[\frac{r}{2GM} \right]_{1/2}^{1/2} \quad \dots (2)$ $= \frac{\pi}{2} \left[\frac{r^3}{2GM} \right]^{1/2} = \frac{2\pi}{4\sqrt{2}} \cdot \left[\frac{r^3}{GM} \right]^{1/2} = \frac{T}{4\sqrt{2}}$ | | |

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| 12. | <p>①</p>  | |
| | <p>Volume of elementary portion = $A dx$</p> <p>Mass of this element $m = (A dx) \rho$</p> <p>Centripetal force = $m \omega^2 x$</p> <p>The centripetal force also represents the pressure difference dp</p> $Adp = m \omega^2 x = \{(A dx) \rho\} \omega^2 x$ $dp = \left(\frac{p}{RT} \right) \omega^2 x dx$ $\frac{dp}{p} = \left(\frac{\omega^2}{RT} \right) \int_0^x x dx$ $\log_e \left(\frac{p}{p_0} \right) = \frac{\omega^2 x^2}{2RT}$ | |
| 13. | <p>②</p> <p>Let $k = \frac{b-a}{L} = \frac{(r+dr)-r}{(x+dx)-x} = \frac{dr}{dx}$</p> $\frac{F}{A} = Y \cdot \frac{dl}{dx} \quad Y = \text{Young's Modulus}$ $dl = \frac{F}{Y \pi r^2} dx = \frac{F}{Y \pi r^2} \frac{dr}{k}$ $l = \int_a^b \frac{F}{Y \pi R} \frac{dr}{r^2} = \frac{F}{Y \pi k} \cdot \frac{(b-a)}{ab} = \frac{F}{Y \pi} \frac{L}{(b-a)} \cdot \frac{(b-a)}{ab}$ $l = \frac{F(L)}{Y \pi ab}$ | |
| 14. | <p>③</p> $P = \frac{1}{2} \rho v^2 \quad (v \rightarrow \text{speed of jet at } B)$ $F = PA = \frac{1}{2} \cdot r \rho A v^2 \Rightarrow F = \frac{1}{2} \rho \cdot \left(\frac{V}{st} \right)^2 A \quad \text{discharge} = V = (sv)t \quad \therefore v = \frac{V}{st}$ $W = FL = \frac{1}{2} \cdot \rho \cdot \left(\frac{V}{st} \right)^2 AL = \frac{1}{2} \cdot \rho \cdot \frac{V^3}{s^2 t^2}$ | |

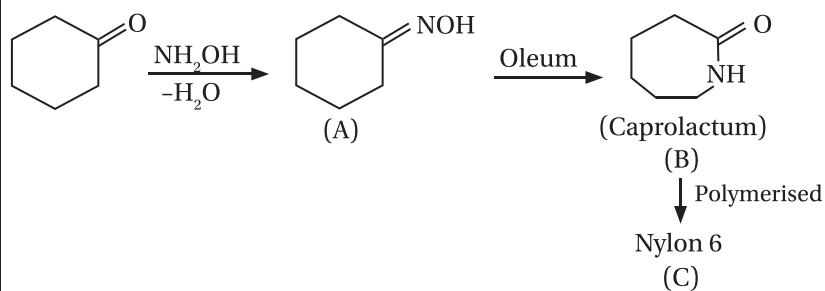
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| 15. | <p>④</p> <p>Difference of levels in the two arms = $x + x \cos \theta$</p> <p>Change in pressure = $\Delta P = x(1 + \cos \theta)\rho g$</p> <p>$\therefore \Delta F = \text{restoring force} = (\Delta p)s = x(1 + \cos \theta)\rho g s = -ma$</p> <p>$\therefore a = -\frac{x(1 + \cos \theta)\rho g s}{m} = -\omega^2 x$</p> <p>$\omega = \sqrt{\frac{(1 + \cos \theta)\rho g s}{m}} = \frac{2\pi}{T}$</p> <p>$\therefore T = 2\pi \sqrt{\frac{m}{(1 + \cos \theta)\rho g s}}$</p> | |
| 16. | <p>②</p> $\cos 2\theta = 2\cos^2 \theta - 1$ <p>$y = 2 \cdot (\cos t + 1) \sin 1000t = 2 \cos t \sin(1000)t + 2 \sin 1000t$ [Formula : $2\sin A \cos B = \sin(A + B) + \sin(A - B)$]</p> <p>$y = \sin(1001)t + \sin(999t) + 2\sin(1000t)$</p> | |
| 17. | <p>③</p> $T = T_0 + \alpha \left(\frac{R^2 T^2}{P^2} \right) \Rightarrow P = \sqrt{\alpha \cdot RT(T - T_0)^{-1/2}} \quad \dots (1)$ <p>$\frac{dp}{dT} = 0$ for minimum pressure</p> <p>$\Rightarrow T = 2T_0$</p> <p>$\therefore P_{\min} = 2R\sqrt{\alpha T_0}$</p> | |
| 18. | <p>①</p> $P = -kA \cdot \frac{d\theta}{dr} = -k4\pi r^2 \left(\frac{d\theta}{dr} \right)$ <p>or, $d\theta = -\frac{p dr}{4\pi k r^2}$</p> $\int_{\theta_1}^{\theta_2} d\theta = -\frac{p}{4\pi k} \int_{r_1}^{r_2} \frac{dr}{r^2}$ $\theta_1 - \theta_2 = \frac{p}{4\pi k} \cdot \frac{r_2 - r_1}{r_1 \cdot r_2}$ $T = \frac{p}{4\pi k} \cdot \frac{(r_2 - r_1)}{R^2}$ $r_2 - r_1 = 4\pi k R^2 T / p$ | |

[5]

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| 19. | <p>③</p> $E = \frac{1}{4\pi\epsilon_0} \cdot \frac{qz}{(R^2 + z^2)^{3/2}} \quad E = 0 \text{ when } z = 0$ <p>direction of electric field will be away from the centre of ring.</p> | |
| 20. | <p>②</p> $C_{AB} = C + C = 2C = \frac{2A\epsilon_0}{d}$ | |
| <p>SECTION B</p> <p>Section B consists of 5 questions of 4 marks each.</p> | | |
| 21. | $\frac{t_1 \cdot t_2}{t_1 + t_2} = \frac{3 \times 6}{9} = 2 \text{ min}$ | |
| 22. | $B_{net} = \frac{\mu_0}{4\pi} \cdot \left[\frac{2i_2}{b} - \frac{2i_1}{a} \right] = 0$ | |
| 23. | $B_{11} = \frac{2M}{d^3} \left(\frac{\mu_0}{4\pi} \right); B_1 = \frac{M}{d^3} \cdot \frac{\mu_0}{4\pi}$ $B_{11} : B_1 = 2 : 1$ | |
| 24. | $e = B \cdot \frac{1}{2} \cdot \frac{r \cdot r d\theta}{dt} = \frac{1}{2} Br^2 \frac{d\theta}{dt} = \frac{1}{2} \cdot Br^2 \omega = \frac{1}{k} Br^2 \omega$ $\therefore k = 2$ | |
| 25. | $\sin i = \sqrt{2} \sin 30^\circ = \sqrt{2} \times \frac{1}{2} = \frac{1}{\sqrt{2}}$ $i = 45^\circ$ | |

CHEMISTRY**SECTION A****Section A consists of 20 questions of 4 mark each.**

26. ②



27. ③

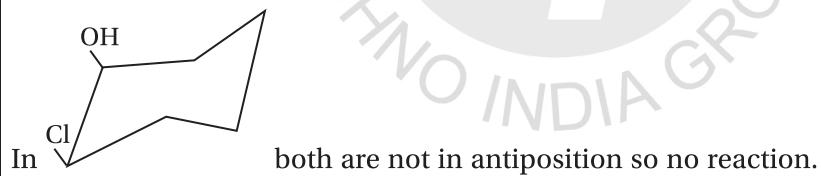
In solid N_2O_5 exist as $[\text{NO}_2^+] [\text{NO}_3^-]$ (nitronium nitrate)

$$\text{For } \text{NO}_2^+, \text{H} = \frac{1}{2}(\text{V} + \text{M} - \text{C} + \text{A}) = \frac{1}{2}(5 + 0 - 1 + 0) = \frac{1}{2} \times 4 = 2 \Rightarrow \text{sp}$$

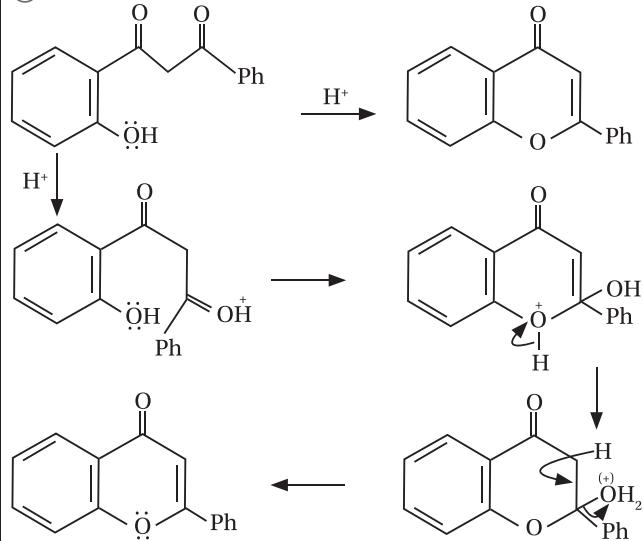
$$\text{For } \text{NO}_3^-, \text{H} = \frac{1}{2}(5 + 0 - 0 + 1) = \frac{6}{2} = 3 \Rightarrow \text{sp}^2$$

28. ④

In 1, 2 disubstituted cyclohexane derivative neighbouring group participation occur only if groups are anti to each other.



29. ③

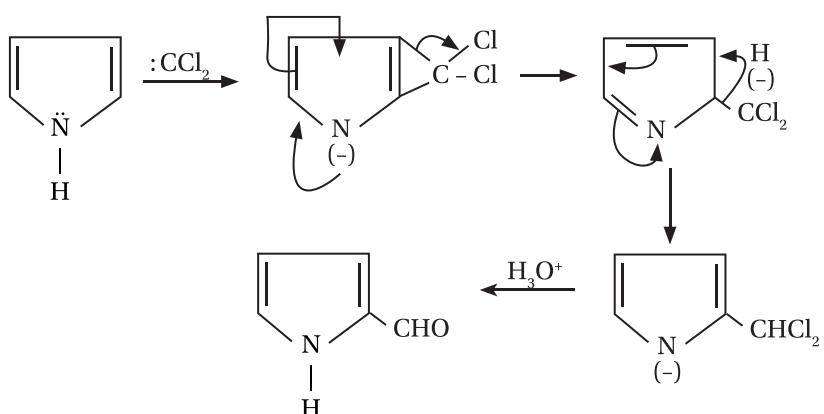
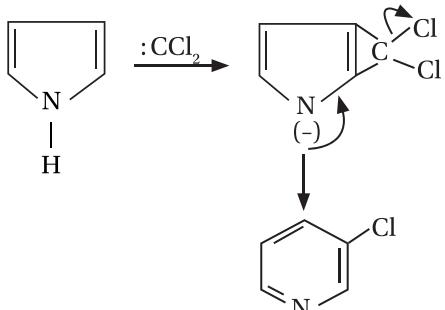


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| 30. | <p>②</p> $K(s) + \frac{1}{2}H_2(s) + \frac{1}{2}O_2(g) \longrightarrow KOH(s); \Delta H = ?$ <p>eq. (1) $K(s) + H_2O(l) \longrightarrow KOH(aq) + \frac{1}{2}H_2(g); \Delta H = -48 \text{ KCal}$</p> <p>eq. (2) $H_2(s) + \frac{1}{2}O_2(s) \longrightarrow H_2O(l); \Delta H = -68.4 \text{ KCal}$</p> <p>eq. (3) $KOH(s) + H_2O \longrightarrow KOH(aq); \Delta H = -14.0 \text{ KCal}$</p> <p>eq. (4) $KOH(aq) \longrightarrow KOH(s) + H_2O; \Delta H = +14.0 \text{ KCal}$</p> <p>Now, eq. (1) + (2) + (4)</p> $K(s) + \frac{1}{2}H_2(s) + \frac{1}{2}O_2(s) \longrightarrow KOH(s)$ $\therefore \Delta H = -48 + (-68.4) + 14.0$ $= -102.4 \text{ KCal}$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 31. | <p>②</p> <p>$Na_2S_2O_3 \cdot 5H_2O$ solution is titrated with I_2 solution.</p> <p>Equivalent weight of $K_2Cr_2O_7 = \frac{M}{6} = \frac{294.16}{6} = 49.03$</p> <p>Milliequivalent of $K_2Cr_2O_7 = \frac{1}{25} \times 32 = 1.28$</p> <p>$\therefore N_1 V_1 = \frac{32}{25}$</p> <p>$N_1 = \frac{32}{250}; M = \frac{32}{250 \times 6} = \frac{8}{375}$</p> | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 32. | <p>④</p> <table style="width: 100%; text-align: center;"> <tr> <td style="width: 30%;"> $CH_3 - C \equiv C - CH_3$ </td> <td style="width: 10%;">$\xrightarrow{Na/NH_3}$</td> <td style="width: 60%; text-align: right;"> CH_3 \diagdown $C = C$ \diagup CH_3 (Trans-2-butene-2) </td> </tr> <tr> <td>Pd/H_2</td> <td>\downarrow</td> <td></td> </tr> <tr> <td>Lindlar's catalyst</td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td style="text-align: right;">A'</td> </tr> <tr> <td></td> <td></td> <td style="text-align: right;">$\mu = O$</td> </tr> <tr> <td></td> <td></td> <td style="text-align: right;">More melting point</td> </tr> <tr> <td>H_3C \diagdown $C = C$ \diagup CH_3</td> <td></td> <td></td> </tr> <tr> <td>Cis butene-2</td> <td></td> <td></td> </tr> <tr> <td>$\mu \neq O$</td> <td></td> <td></td> </tr> <tr> <td>More boiling point</td> <td></td> <td></td> </tr> </table> | $CH_3 - C \equiv C - CH_3$ | $\xrightarrow{Na/NH_3}$ | CH_3 \diagdown $C = C$ \diagup CH_3 (Trans-2-butene-2) | Pd/H_2 | \downarrow | | Lindlar's catalyst | | | | | A' | | | $\mu = O$ | | | More melting point | H_3C \diagdown $C = C$ \diagup CH_3 | | | Cis butene-2 | | | $\mu \neq O$ | | | More boiling point | | |
| $CH_3 - C \equiv C - CH_3$ | $\xrightarrow{Na/NH_3}$ | CH_3 \diagdown $C = C$ \diagup CH_3 (Trans-2-butene-2) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Pd/H_2 | \downarrow | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Lindlar's catalyst | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | A' | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | $\mu = O$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | More melting point | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| H_3C \diagdown $C = C$ \diagup CH_3 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Cis butene-2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| $\mu \neq O$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| More boiling point | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 33. | <p>④</p> <p>All of these ①, ②, & ③ are correct.</p> | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

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| 34. | <p>①</p> |
| 35. | <p>①</p> $E_{\text{cell}} = E_{\text{cell}}^{\circ} - \frac{0.059}{2} \log \frac{(\text{Zn}^{++})}{(\text{Cu}^{++})}$ $= 1.18 + \frac{0.059}{2} \log \frac{(\text{Cu}^{++})}{(\text{Zn}^{++})}$ <p>To make cell reaction spontaneous, $E_{\text{cell}} = +\text{ve}$,</p> <p>i.e. $\frac{0.059}{2} \log_{10} \frac{(\text{Cu}^{++})}{(\text{Zn}^{++})} > 1.18$</p> $\log_{10} [\text{Cu}^{++}] > \frac{2.36}{0.059}$ $\Rightarrow \log_{10} [\text{Cu}^{++}] > 40$ $\therefore (\text{Cu}^{++}) > 10^{-40}$ |
| 36. | <p>②</p> <p>Energy of photon $= h\nu = h\frac{c}{\lambda}$</p> $= \frac{6.625 \times 10^{-34} \times 3 \times 10^8}{5000 \times 10^{-10}} \text{ J}$ $= 3.975 \times 10^{-19} \text{ J}$ <p>Energy emitted by bulb $= 150 \times \frac{10}{100} \text{ J/S}$</p> $150 \times \frac{10}{100} = n \times 3.975 \times 10^{-19}$ $\Rightarrow n = 3.77 \times 10^{19}$ |

37. ④

Normal Reaction:

Abnormal Reaction:
(Ring Expansion)

38. ③

$$\Lambda_m^{\circ} = \lambda_{\text{Ag}^+}^{\circ} + \lambda_{\text{Cl}}^{\circ} = x + y$$

$$\Lambda_m^{\circ} = K \times \frac{1000}{S} \Rightarrow S = \frac{K}{\Lambda_m^{\circ}} \times 1000$$

$$\Rightarrow \frac{K}{(x+y)} 1000$$

Solubility (S) in gm/litre

$$= S \times 143.5$$

$$S_1 = \frac{K \times 1000 \times 143.5}{x+y}$$

39. ④

$$\log_{10} \left(\frac{K_L}{K_1} \right) = \frac{E_a}{2.303} R \left[\frac{1}{T_1} - \frac{1}{T_2} \right]$$

$$\Rightarrow \log_{10} \left(\frac{4.5 \times 10^7}{1.5 \times 10^7} \right) = \frac{E_a}{2.303 \times 8.34} \left[\frac{1}{323} - \frac{1}{373} \right]$$

$$\Rightarrow E_a = 2.2 \times 10^4 \text{ J(mole)}^{-1}$$

40. ④

NaHCO_3 reaction takes place with highly acidic groups like $-\overset{\text{O}}{\parallel}\text{C}-\text{OH}$, $-\text{SO}_3\text{H}$ etc.

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| 41. | <p>③</p> $\text{NaNO}_3 : \text{NaNO}_3 \xleftarrow{\Delta} \text{NaNO}_2 + \frac{1}{2}\text{O}_2 \uparrow$ $\text{Cu}(\text{NO}_3)_2 \xrightarrow{\Delta} \text{CuO} + 2\text{NO}_2 \uparrow + \frac{1}{2}\text{O}_2 \uparrow$ $\text{Hg}(\text{NO}_3)_2 \xrightarrow{\Delta} \text{Hg} \downarrow + 2\text{NO}_2 \uparrow + \frac{1}{2}\text{O}_2 \uparrow$ $\text{AgNO}_3 \xrightarrow{\Delta} \text{Ag} + \text{NO}_2 \uparrow + \frac{1}{2}\text{O}_2 \uparrow$ |
| 42. | <p>④</p> $\frac{P_A^0 - P_A}{P_A^0} = x_B \Rightarrow \frac{W_2}{W_1 + W_2} = \frac{WM}{mW}$ $\Rightarrow \frac{0.04}{2.54} = \frac{5 \times 18}{m \times 80} \Rightarrow m = 70.3$ |
| 43. | <p>①</p> <p>This is an example of intramolecular electrophilic substitution reaction.</p> |
| 44. | <p>①</p> $E_{\text{cell}}^0 = 0.25 + 0.34 = 0.59\text{V}$ $E_{\text{cell}}^0 = \frac{0.059}{2} \log K_C = 0.59$ $\therefore \log K_C = 20 \Rightarrow K_C = 10^{20}$ |
| 45. | <p>③</p> |

SECTION B

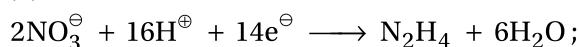
Section B consists of 5 questions of 4 marks each.

46. ($n = 6$)

$$\text{At, } r = r_6, \psi^2 2s = 0 \quad \text{So, } \left[2 - \frac{r_0}{3a_0} \right] = 0$$

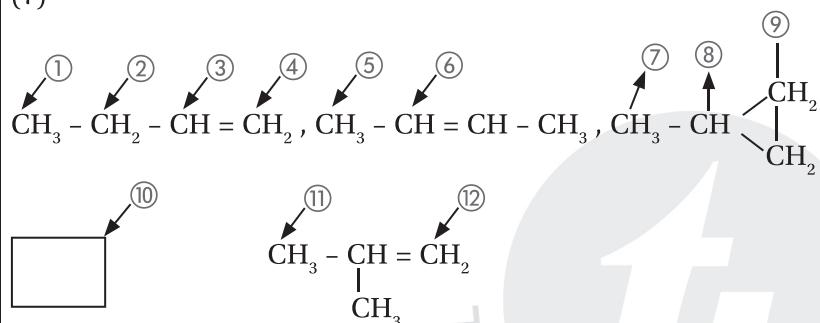
$$r_0 = 6 a_0 \quad \Rightarrow n = 6$$

47. (7)

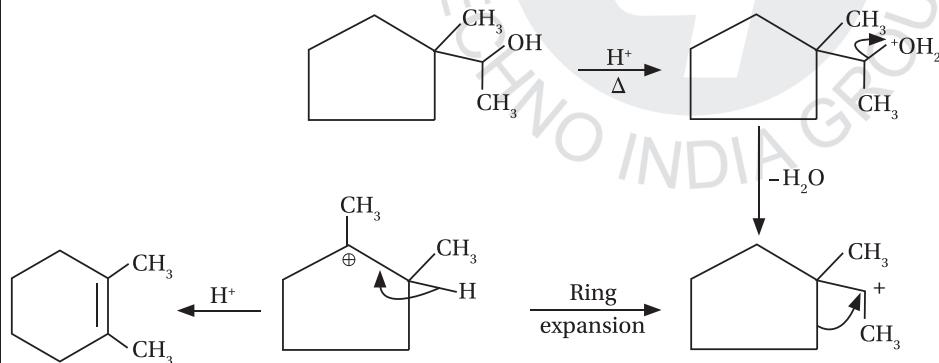


For 1 mole of NO_3^- ion electron required = 7 moles

48. (7)



49. (7)



6C atoms in ring (six membered ring)

+1 π bond = 7

50. (3)

$$\left(\frac{t_2}{t_1} \right) = \left(\frac{a_1}{a_2} \right)^{n-1}$$

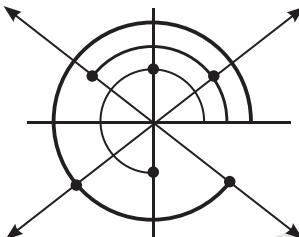
$$\Rightarrow 16 = \left(\frac{1}{\frac{1}{4}} \right)^{n-1}$$

$\Rightarrow n = 3$, third order reaction

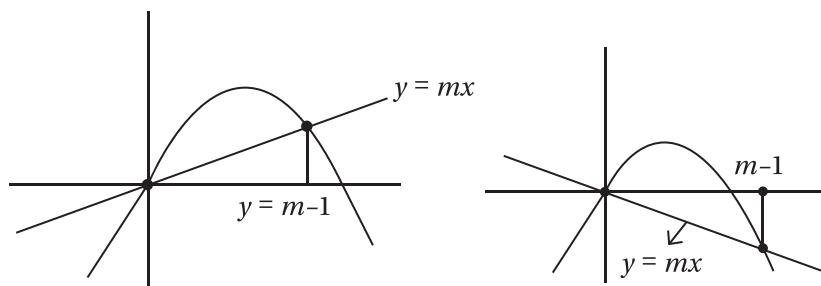
MATHEMATICS

SECTION A

Section A consists of 20 questions of 4 mark each.

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| 51. (4) $f(x) = -4\sin^3x - 3\sin^2x + 3\sin x + 5$ $f'(x) = -12\sin^2x \cos x - 6\sin x \cdot \cos x + 3\cos x$ $= -3\cos x(4\sin^2x + 2\sin x - 1)$  <p style="margin-left: 200px;">$\cos x = 0$ 2 solution</p> <p style="margin-left: 200px;">$4\sin^2x + 2\sin x - 1 = 0$</p> $\sin x = \frac{-1-\sqrt{5}}{4}, \frac{-1+\sqrt{5}}{4}$ <p style="margin-left: 200px;">2 solution 2 solution</p> <p># 6 solution.</p> |
| 52. (2) $ \vec{a} + \vec{b} + \vec{c} ^2 = \vec{d} ^2$ $\Rightarrow 1 + 4 + 6 + 2(\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}) = 2$ $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a} = -\frac{19}{2}$ |
| 53. (1) <p>For identity $a = b = c = 0$</p> $p^2 - 3p + 2 = 0 \cap (p-1)^2 = 0 \cap p^2 - 4p + 3 = 0 \Rightarrow p = 1$ |
| 54. (3) $I = \int_0^{\pi/6} \frac{\sqrt{\cos 3x}}{\sin 3x + \sqrt{\cos 3x}} dx \quad \dots (1)$ <p style="text-align: center;">$\left(u \text{ sin } g : \int_0^a f(x) dx = \int_0^a f(a-x) dx \right)$</p> $\cos 3\left(\frac{\pi}{6} - x\right) = \sin 3x \quad \dots (2)$ $= \int_0^{\pi/6} \frac{\sqrt{\sin 3x}}{\sqrt{\cos 3x + \sqrt{\sin 3x}}} dx \quad \dots (2)$ $(1) + (2) : 2I = \int_0^{\pi/6} dx = \frac{\pi}{6} \Rightarrow I = \frac{\pi}{12}$ |

55. ③



$$\left| \int_0^{m-1} (x - x^2) mx dx \right| = \frac{9}{2}$$

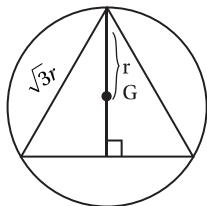
After solving we get
two values of m.
 $m = -2, 4$

56. ①

Using leibnitz Rule:

$$\begin{aligned} 2y \cdot \frac{dy}{dx} e^{y^2} - 1 \cdot \tan x &= \frac{1}{x} \\ \frac{dy}{dx} &= \frac{\left(\tan x + \frac{1}{x} \right)}{2y} e^{-y^2} \\ \Rightarrow \frac{dy}{dx} &= \left(\frac{x \tan x + 1}{2ny} \right) e^{-y^2} \end{aligned}$$

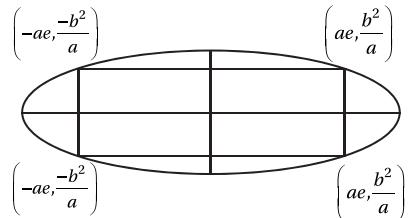
57. ③



$$\begin{aligned} \frac{d}{dt}(2\pi r) &= \pi \\ 2\pi \cdot \frac{dr}{dt} = \pi &\Rightarrow \frac{dr}{dt} = \frac{1}{2} \end{aligned}$$

$$\begin{aligned} \frac{d}{dt}(3a) &= \\ \frac{d}{dt}(3 \cdot \sqrt{3}r) &= 3\sqrt{3} \cdot \frac{dr}{dt} = \frac{3\sqrt{3}}{2} \end{aligned}$$

58. ②

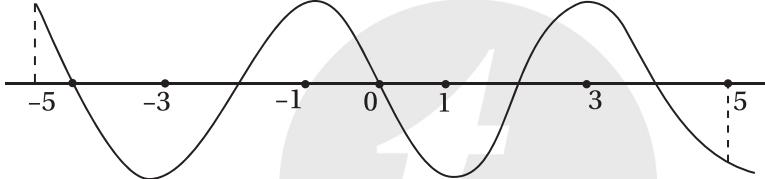
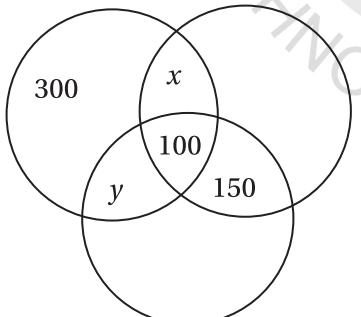


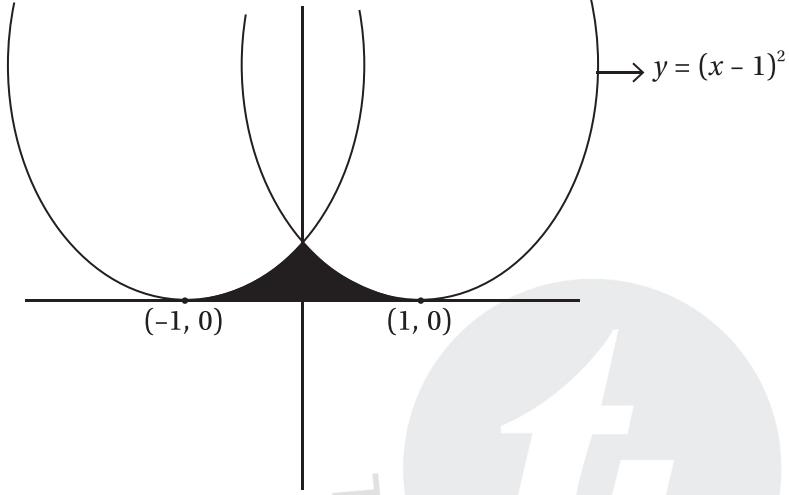
$$\begin{aligned} Now, b^2 &= a^2(1 - e^2) \\ &= 50^2 \left(1 - \frac{1}{4} \right) \\ &= 50^2 \times \frac{3}{4} \end{aligned}$$

$$Area = 4b^2 e$$

$$\begin{aligned} &= 4 \times b^2 \times \frac{1}{2} \\ &= 2b^2 \end{aligned}$$

$$= 2 \times 50^2 \times \frac{3}{4} = 3750$$

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| 59. | <p>(2)</p> $ A = 0$ $(\sin x + 4 \cos x) \sin y + 3 \cos y = \sqrt{26}$ It is possible if $(\sin x + 4 \cos x)^2 + 9 = 26$ $\Rightarrow \cos x(15 \cos x + 8 \sin x) = 16$ |
| 60. | <p>(1)</p> $\frac{1}{x} [(1+x)^{101} - 1]$ Coeff of x^7 in $\frac{1}{x} [(1+x)^{101} - 1]$ $= \text{Coeff of } x^8 \text{ in } (1+x)^{101} = {}^{101}C_8 = {}^{101}C_{93}$ |
| 61. | <p>(1)</p>  <p>$f(0) = 0$ ($\because f(x)$ is odd function) Minimum five real roots.</p> |
| 62. | <p>(2)</p>  $\begin{aligned} x + y + 150 \\ = 100 + 150 \\ = 250 \end{aligned}$ |
| 63. | <p>(3)</p> <p>(A) $A \cdot A^t = I \Rightarrow A A^t = I \Rightarrow A ^2 = 1$ (True) always invertible. $\Rightarrow A = \pm 1$ $\Rightarrow A^{-1}$ exist.</p> <p>(B) $A^t = -A$ $A^t = -A \Rightarrow A = - A \Rightarrow 2 A = 0 \Rightarrow A = 0$ non invertible (True)</p> <p>(C) $A^2 = A \Rightarrow A ^2 = A$ $\Rightarrow A (A - 1) = 0$ $\Rightarrow A = 0, \text{ or } A = 1$ not always invertible. (False)</p> <p>(D) $A^2 = I \Rightarrow A = \pm 1$ True always invertible (true)</p> |

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| 64. | <p>① $(\lambda, 5-\lambda)$ be any point on the line. Equation of chord of contact $T = 0$</p> $\begin{aligned}\lambda x + y(5 - \lambda) &= 2 \\ \Rightarrow (5y - 2) + \lambda(x - y) &= 0 \\ \Rightarrow y = \frac{5}{2} \quad \text{and} \quad x = y = \frac{5}{2} \quad \therefore \text{Point of intersection is } \left(\frac{5}{2}, \frac{5}{2}\right)\end{aligned}$ |
| 65. | <p>②</p>  $y = (x - 1)^2$ $I = 2 \int_0^1 (x - 1)^2 dx = \frac{2}{3}$ |
| 66. | <p>②</p> $\frac{T_n}{t_n} = \frac{A + (n-1)D}{a + (n-1)d} = \frac{n+1}{3n-2} \quad \text{put } n=3 \Rightarrow \frac{S_5}{s_5} = \frac{4}{7}$ |
| 67. | <p>②</p> $\left. \begin{aligned} \sigma^2(an+b) &= a^2\sigma^2 \text{ (For variance)} \\ \bar{y} &= \overline{(ax+b)} = a\bar{x} + b \text{ (for Mean)} \end{aligned} \right\} \begin{aligned} \text{Variance} &= 2^2 a^2 \\ \text{Mean} &= 2\bar{x} \end{aligned}$ |
| 68. | <p>④</p> $\begin{aligned} ydx + xdy + \sin x \cos^2(xy) dx + \sin y \cos^2(xy) dy &= 0 \\ \Rightarrow \frac{d(xy)}{\cos^2(xy)} + \sin x dx + \sin y dy &= 0 \\ \Rightarrow \tan(xy) - \cos x - \cos y &= c \end{aligned}$ |
| 69. | <p>③</p> $\begin{aligned} 4t_1 t_2 &= 9 ; 4(t_1 + t_2) = b \\ b^2 &= 16(t_1 + t_2)^2 = 16 \left[(t_1 - t_2)^2 + 4t_1 t_2 \right] = 16(t_1 - t_2)^2 + 144 > 144 \\ b > 12 \quad \Rightarrow \quad b_{\min} &= 13 \end{aligned}$ |

[16]

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| 70. (3) $x^2 - 2 x \geq 0 \cap -1 \leq \frac{x}{4} \leq 1$ $\Rightarrow x = 0, -2 \leq x \cup x \geq 2 \cap -4 \leq x \leq 4$ $\Rightarrow [-4, -2] \cup \{0\} \cup [2, 4]$ |
| SECTION B |
| Section B consists of 5 questions of 4 marks each. |
| 71. (5) $\frac{x^2 \frac{1}{x^4} + \frac{1}{x^4} + x^3 + \frac{ax}{3} + \frac{ax}{3} + \frac{ax}{3}}{7} \geq \left(\frac{a^3}{27} \right)$ $\Rightarrow 7 \left(\frac{a^3}{27} \right)^{\frac{1}{7}} = 9 - b \Rightarrow a = 3, b = 2$ |
| 72. (2) $\frac{b}{a} = \frac{1}{\sqrt{3}} = e$ $\frac{1}{e^2} + \frac{1}{(e')^2} = 1 \Rightarrow (e')^2 = 4 \Rightarrow e' = 2$ |
| 73. (9) <div style="display: flex; justify-content: space-between; align-items: flex-start;"> <div style="flex: 1;"> $\vec{a} = \lambda \hat{i} + 2 \hat{j} + \hat{k}$ $[\vec{a} \vec{b} \vec{c}] = 0$ $\Rightarrow \begin{vmatrix} -1 & 0 & 0 \\ -2 & 3 & 2 \\ \lambda & 2-\lambda & 1 \end{vmatrix} = 0 \Rightarrow \lambda = \frac{1}{2} \Rightarrow 18\lambda = 9$ </div> </div> |
| 74. Using Baye's theorem. $\text{Required prob} = \frac{\frac{2}{6} \times 1}{\frac{3}{6} \times 0 + \frac{1}{6} \times \frac{1}{2} + \frac{2}{6} \times 1} = \frac{4}{5}$ $\therefore a + b = 4 + 5 = 9$ |
| 75. (2) $\frac{x-5}{3-5} = \frac{y-1}{\beta-1} = \frac{z-\alpha}{1-\alpha}$ $\frac{-5}{-2} = \frac{\frac{17}{2}-1}{\beta-1} = \frac{\frac{-13}{2}-\alpha}{1-\alpha} \Rightarrow \alpha = 6, \beta = 4$ $\alpha - \beta = 6 - 4 = 2$ |